

## Measurements of Neutral $B$ Decay Branching Fractions to $K_s^0\pi^+\pi^-$ Final States

B. Aubert,<sup>1</sup> R. Barate,<sup>1</sup> D. Boutigny,<sup>1</sup> F. Couderc,<sup>1</sup> J.-M. Gaillard,<sup>1</sup> A. Hicheur,<sup>1</sup> Y. Karyotakis,<sup>1</sup> J. P. Lees,<sup>1</sup>  
V. Tisserand,<sup>1</sup> A. Zghiche,<sup>1</sup> A. Palano,<sup>2</sup> A. Pompili,<sup>2</sup> J. C. Chen,<sup>3</sup> N. D. Qi,<sup>3</sup> G. Rong,<sup>3</sup> P. Wang,<sup>3</sup> Y. S. Zhu,<sup>3</sup>  
G. Eigen,<sup>4</sup> I. Ofte,<sup>4</sup> B. Stugu,<sup>4</sup> G. S. Abrams,<sup>5</sup> A. W. Borgland,<sup>5</sup> A. B. Breon,<sup>5</sup> D. N. Brown,<sup>5</sup> J. Button-Shafer,<sup>5</sup>  
R. N. Cahn,<sup>5</sup> E. Charles,<sup>5</sup> C. T. Day,<sup>5</sup> M. S. Gill,<sup>5</sup> A. V. Gritsan,<sup>5</sup> Y. Groysman,<sup>5</sup> R. G. Jacobsen,<sup>5</sup> R. W. Kadel,<sup>5</sup>  
J. Kadyk,<sup>5</sup> L. T. Kerth,<sup>5</sup> Yu. G. Kolomensky,<sup>5</sup> G. Kukartsev,<sup>5</sup> G. Lynch,<sup>5</sup> L. M. Mir,<sup>5</sup> P. J. Oddone,<sup>5</sup>  
T. J. Orimoto,<sup>5</sup> M. Pripstein,<sup>5</sup> N. A. Roe,<sup>5</sup> M. T. Ronan,<sup>5</sup> V. G. Shelkov,<sup>5</sup> W. A. Wenzel,<sup>5</sup> M. Barrett,<sup>6</sup>  
K. E. Ford,<sup>6</sup> T. J. Harrison,<sup>6</sup> A. J. Hart,<sup>6</sup> C. M. Hawkes,<sup>6</sup> S. E. Morgan,<sup>6</sup> A. T. Watson,<sup>6</sup> M. Fritsch,<sup>7</sup> K. Goetzen,<sup>7</sup>  
T. Held,<sup>7</sup> H. Koch,<sup>7</sup> B. Lewandowski,<sup>7</sup> M. Pelizaeus,<sup>7</sup> M. Steinke,<sup>7</sup> J. T. Boyd,<sup>8</sup> N. Chevalier,<sup>8</sup> W. N. Cottingham,<sup>8</sup>  
M. P. Kelly,<sup>8</sup> T. E. Latham,<sup>8</sup> F. F. Wilson,<sup>8</sup> T. Cuhadar-Donszelmann,<sup>9</sup> C. Hearty,<sup>9</sup> N. S. Knecht,<sup>9</sup> T. S. Mattison,<sup>9</sup>  
J. A. McKenna,<sup>9</sup> D. Thiessen,<sup>9</sup> A. Khan,<sup>10</sup> P. Kyberd,<sup>10</sup> L. Teodorescu,<sup>10</sup> A. E. Blinov,<sup>11</sup> V. E. Blinov,<sup>11</sup>  
V. P. Druzhinin,<sup>11</sup> V. B. Golubev,<sup>11</sup> V. N. Ivanchenko,<sup>11</sup> E. A. Kravchenko,<sup>11</sup> A. P. Onuchin,<sup>11</sup> S. I. Serebnyakov,<sup>11</sup>  
Yu. I. Skovpen,<sup>11</sup> E. P. Solodov,<sup>11</sup> A. N. Yushkov,<sup>11</sup> D. Best,<sup>12</sup> M. Bruinsma,<sup>12</sup> M. Chao,<sup>12</sup> I. Eschrich,<sup>12</sup>  
D. Kirkby,<sup>12</sup> A. J. Lankford,<sup>12</sup> M. Mandelkern,<sup>12</sup> R. K. Mommsen,<sup>12</sup> W. Roethel,<sup>12</sup> D. P. Stoker,<sup>12</sup> C. Buchanan,<sup>13</sup>  
B. L. Hartfiel,<sup>13</sup> S. D. Foulkes,<sup>14</sup> J. W. Gary,<sup>14</sup> B. C. Shen,<sup>14</sup> K. Wang,<sup>14</sup> D. del Re,<sup>15</sup> H. K. Hadavand,<sup>15</sup>  
E. J. Hill,<sup>15</sup> D. B. MacFarlane,<sup>15</sup> H. P. Paar,<sup>15</sup> Sh. Rahatlou,<sup>15</sup> V. Sharma,<sup>15</sup> J. W. Berryhill,<sup>16</sup> C. Campagnari,<sup>16</sup>  
B. Dahmes,<sup>16</sup> O. Long,<sup>16</sup> A. Lu,<sup>16</sup> M. A. Mazur,<sup>16</sup> J. D. Richman,<sup>16</sup> W. Verkerke,<sup>16</sup> T. W. Beck,<sup>17</sup> A. M. Eisner,<sup>17</sup>  
C. A. Heusch,<sup>17</sup> J. Kroseberg,<sup>17</sup> W. S. Lockman,<sup>17</sup> G. Nesom,<sup>17</sup> T. Schalk,<sup>17</sup> B. A. Schumm,<sup>17</sup> A. Seiden,<sup>17</sup>  
P. Spradlin,<sup>17</sup> D. C. Williams,<sup>17</sup> M. G. Wilson,<sup>17</sup> J. Albert,<sup>18</sup> E. Chen,<sup>18</sup> G. P. Dubois-Felsmann,<sup>18</sup>  
A. Dvoretzskii,<sup>18</sup> D. G. Hitlin,<sup>18</sup> I. Narsky,<sup>18</sup> T. Piatenko,<sup>18</sup> F. C. Porter,<sup>18</sup> A. Ryd,<sup>18</sup> A. Samuel,<sup>18</sup> S. Yang,<sup>18</sup>  
S. Jayatilake,<sup>19</sup> G. Mancinelli,<sup>19</sup> B. T. Meadows,<sup>19</sup> M. D. Sokoloff,<sup>19</sup> T. Abe,<sup>20</sup> F. Blanc,<sup>20</sup> P. Bloom,<sup>20</sup>  
S. Chen,<sup>20</sup> W. T. Ford,<sup>20</sup> U. Nauenberg,<sup>20</sup> A. Olivas,<sup>20</sup> P. Rankin,<sup>20</sup> J. G. Smith,<sup>20</sup> J. Zhang,<sup>20</sup> L. Zhang,<sup>20</sup>  
A. Chen,<sup>21</sup> J. L. Harton,<sup>21</sup> A. Soffer,<sup>21</sup> W. H. Toki,<sup>21</sup> R. J. Wilson,<sup>21</sup> Q. L. Zeng,<sup>21</sup> D. Altenburg,<sup>22</sup> T. Brandt,<sup>22</sup>  
J. Brose,<sup>22</sup> M. Dickopp,<sup>22</sup> E. Feltresi,<sup>22</sup> A. Hauke,<sup>22</sup> H. M. Lacker,<sup>22</sup> R. Müller-Pfefferkorn,<sup>22</sup> R. Nogowski,<sup>22</sup>  
S. Otto,<sup>22</sup> A. Petzold,<sup>22</sup> J. Schubert,<sup>22</sup> K. R. Schubert,<sup>22</sup> R. Schwierz,<sup>22</sup> B. Spaan,<sup>22</sup> J. E. Sundermann,<sup>22</sup>  
D. Bernard,<sup>23</sup> G. R. Bonneaud,<sup>23</sup> F. Brochard,<sup>23</sup> P. Grenier,<sup>23</sup> S. Schrenk,<sup>23</sup> Ch. Thiebaux,<sup>23</sup> G. Vasileiadis,<sup>23</sup>  
M. Verderi,<sup>23</sup> D. J. Bard,<sup>24</sup> P. J. Clark,<sup>24</sup> D. Lavin,<sup>24</sup> F. Muheim,<sup>24</sup> S. Playfer,<sup>24</sup> Y. Xie,<sup>24</sup> M. Andreotti,<sup>25</sup>  
V. Azzolini,<sup>25</sup> D. Bettoni,<sup>25</sup> C. Bozzi,<sup>25</sup> R. Calabrese,<sup>25</sup> G. Cibinetto,<sup>25</sup> E. Luppi,<sup>25</sup> M. Negrini,<sup>25</sup> L. Piemontese,<sup>25</sup>  
A. Sarti,<sup>25</sup> E. Treadwell,<sup>26</sup> F. Anulli,<sup>27</sup> R. Baldini-Ferrolì,<sup>27</sup> A. Calcaterra,<sup>27</sup> R. de Sangro,<sup>27</sup> G. Finocchiaro,<sup>27</sup>  
P. Patteri,<sup>27</sup> I. M. Peruzzi,<sup>27</sup> M. Piccolo,<sup>27</sup> A. Zallo,<sup>27</sup> A. Buzzo,<sup>28</sup> R. Capra,<sup>28</sup> R. Contri,<sup>28</sup> G. Crosetti,<sup>28</sup>  
M. Lo Vetere,<sup>28</sup> M. Macri,<sup>28</sup> M. R. Monge,<sup>28</sup> S. Passaggio,<sup>28</sup> C. Patrignani,<sup>28</sup> E. Robutti,<sup>28</sup> A. Santroni,<sup>28</sup>  
S. Tosi,<sup>28</sup> S. Bailey,<sup>29</sup> G. Brandenburg,<sup>29</sup> K. S. Chaisanguanthum,<sup>29</sup> M. Morii,<sup>29</sup> E. Won,<sup>29</sup> R. S. Dubitzky,<sup>30</sup>  
U. Langenegger,<sup>30</sup> W. Bhimji,<sup>31</sup> D. A. Bowerman,<sup>31</sup> P. D. Dauncey,<sup>31</sup> U. Egede,<sup>31</sup> J. R. Gaillard,<sup>31</sup> G. W. Morton,<sup>31</sup>  
J. A. Nash,<sup>31</sup> M. B. Nikolich,<sup>31</sup> G. P. Taylor,<sup>31</sup> M. J. Charles,<sup>32</sup> G. J. Grenier,<sup>32</sup> U. Mallik,<sup>32</sup> J. Cochran,<sup>33</sup>  
H. B. Crawley,<sup>33</sup> J. Lamsa,<sup>33</sup> W. T. Meyer,<sup>33</sup> S. Prell,<sup>33</sup> E. I. Rosenberg,<sup>33</sup> A. E. Rubin,<sup>33</sup> J. Yi,<sup>33</sup> M. Biasini,<sup>34</sup>  
R. Covarelli,<sup>34</sup> M. Pippi,<sup>34</sup> M. Davier,<sup>35</sup> X. Giroux,<sup>35</sup> G. Grosdidier,<sup>35</sup> A. Höcker,<sup>35</sup> S. Laplace,<sup>35</sup> F. Le Diberder,<sup>35</sup>  
V. Lepeltier,<sup>35</sup> A. M. Lutz,<sup>35</sup> T. C. Petersen,<sup>35</sup> S. Plaszczynski,<sup>35</sup> M. H. Schune,<sup>35</sup> L. Tantot,<sup>35</sup> G. Wormser,<sup>35</sup>  
C. H. Cheng,<sup>36</sup> D. J. Lange,<sup>36</sup> M. C. Simani,<sup>36</sup> D. M. Wright,<sup>36</sup> A. J. Bevan,<sup>37</sup> C. A. Chavez,<sup>37</sup> J. P. Coleman,<sup>37</sup>  
I. J. Forster,<sup>37</sup> J. R. Fry,<sup>37</sup> E. Gabathuler,<sup>37</sup> R. Gamet,<sup>37</sup> D. E. Hutchcroft,<sup>37</sup> R. J. Parry,<sup>37</sup> D. J. Payne,<sup>37</sup>  
R. J. Sloane,<sup>37</sup> C. Touramanis,<sup>37</sup> J. J. Back,<sup>38,\*</sup> C. M. Cormack,<sup>38</sup> P. F. Harrison,<sup>38,\*</sup> F. Di Lodovico,<sup>38</sup>  
G. B. Mohanty,<sup>38,\*</sup> C. L. Brown,<sup>39</sup> G. Cowan,<sup>39</sup> R. L. Flack,<sup>39</sup> H. U. Flaecher,<sup>39</sup> M. G. Green,<sup>39</sup> P. S. Jackson,<sup>39</sup>  
T. R. McMahon,<sup>39</sup> S. Ricciardi,<sup>39</sup> F. Salvatore,<sup>39</sup> M. A. Winter,<sup>39</sup> D. Brown,<sup>40</sup> C. L. Davis,<sup>40</sup> J. Allison,<sup>41</sup>  
N. R. Barlow,<sup>41</sup> R. J. Barlow,<sup>41</sup> P. A. Hart,<sup>41</sup> M. C. Hodgkinson,<sup>41</sup> G. D. Lafferty,<sup>41</sup> A. J. Lyon,<sup>41</sup> J. C. Williams,<sup>41</sup>  
A. Farbin,<sup>42</sup> W. D. Hulsbergen,<sup>42</sup> A. Jawahery,<sup>42</sup> D. Kovalskyi,<sup>42</sup> C. K. Lae,<sup>42</sup> V. Lillard,<sup>42</sup> D. A. Roberts,<sup>42</sup>  
G. Blaylock,<sup>43</sup> C. Dallapiccola,<sup>43</sup> K. T. Flood,<sup>43</sup> S. S. Hertzbach,<sup>43</sup> R. Kofler,<sup>43</sup> V. B. Koptchev,<sup>43</sup> T. B. Moore,<sup>43</sup>  
S. Saremi,<sup>43</sup> H. Staengle,<sup>43</sup> S. Willocq,<sup>43</sup> R. Cowan,<sup>44</sup> G. Sciolla,<sup>44</sup> S. J. Sekula,<sup>44</sup> F. Taylor,<sup>44</sup> R. K. Yamamoto,<sup>44</sup>

D. J. J. Mangeol,<sup>45</sup> P. M. Patel,<sup>45</sup> S. H. Robertson,<sup>45</sup> A. Lazzaro,<sup>46</sup> V. Lombardo,<sup>46</sup> F. Palombo,<sup>46</sup>  
 J. M. Bauer,<sup>47</sup> L. Cremaldi,<sup>47</sup> V. Eschenburg,<sup>47</sup> R. Godang,<sup>47</sup> R. Kroeger,<sup>47</sup> J. Reidy,<sup>47</sup> D. A. Sanders,<sup>47</sup>  
 D. J. Summers,<sup>47</sup> H. W. Zhao,<sup>47</sup> S. Brunet,<sup>48</sup> D. Côté,<sup>48</sup> P. Taras,<sup>48</sup> H. Nicholson,<sup>49</sup> N. Cavallo,<sup>50,†</sup> F. Fabozzi,<sup>50,†</sup>  
 C. Gatto,<sup>50</sup> L. Lista,<sup>50</sup> D. Monorchio,<sup>50</sup> P. Paolucci,<sup>50</sup> D. Piccolo,<sup>50</sup> C. Sciacca,<sup>50</sup> M. Baak,<sup>51</sup> H. Bulten,<sup>51</sup>  
 G. Raven,<sup>51</sup> H. L. Snoek,<sup>51</sup> L. Wilden,<sup>51</sup> C. P. Jessop,<sup>52</sup> J. M. LoSecco,<sup>52</sup> T. Allmendinger,<sup>53</sup> K. K. Gan,<sup>53</sup>  
 K. Honscheid,<sup>53</sup> D. Hufnagel,<sup>53</sup> H. Kagan,<sup>53</sup> R. Kass,<sup>53</sup> T. Pulliam,<sup>53</sup> A. M. Rahimi,<sup>53</sup> R. Ter-Antonyan,<sup>53</sup>  
 Q. K. Wong,<sup>53</sup> J. Brau,<sup>54</sup> R. Frey,<sup>54</sup> O. Igonkina,<sup>54</sup> C. T. Potter,<sup>54</sup> N. B. Sinev,<sup>54</sup> D. Strom,<sup>54</sup> E. Torrence,<sup>54</sup>  
 F. Colecchia,<sup>55</sup> A. Dorigo,<sup>55</sup> F. Galeazzi,<sup>55</sup> M. Margoni,<sup>55</sup> M. Morandin,<sup>55</sup> M. Posocco,<sup>55</sup> M. Rotondo,<sup>55</sup>  
 F. Simonetto,<sup>55</sup> R. Stroili,<sup>55</sup> G. Tiozzo,<sup>55</sup> C. Voci,<sup>55</sup> M. Benayoun,<sup>56</sup> H. Briand,<sup>56</sup> J. Chauveau,<sup>56</sup> P. David,<sup>56</sup>  
 Ch. de la Vaissière,<sup>56</sup> L. Del Buono,<sup>56</sup> O. Hamon,<sup>56</sup> M. J. J. John,<sup>56</sup> Ph. Leruste,<sup>56</sup> J. Malcles,<sup>56</sup> J. Ocariz,<sup>56</sup>  
 M. Pivk,<sup>56</sup> L. Roos,<sup>56</sup> S. T'Jampens,<sup>56</sup> G. Therin,<sup>56</sup> P. F. Manfredi,<sup>57</sup> V. Re,<sup>57</sup> P. K. Behera,<sup>58</sup> L. Gladney,<sup>58</sup>  
 Q. H. Guo,<sup>58</sup> J. Panetta,<sup>58</sup> C. Angelini,<sup>59</sup> G. Batignani,<sup>59</sup> S. Bettarini,<sup>59</sup> M. Bondioli,<sup>59</sup> F. Bucci,<sup>59</sup> G. Calderini,<sup>59</sup>  
 M. Carpinelli,<sup>59</sup> F. Forti,<sup>59</sup> M. A. Giorgi,<sup>59</sup> A. Lusiani,<sup>59</sup> G. Marchiori,<sup>59</sup> F. Martinez-Vidal,<sup>59,‡</sup> M. Morganti,<sup>59</sup>  
 N. Neri,<sup>59</sup> E. Paoloni,<sup>59</sup> M. Rama,<sup>59</sup> G. Rizzo,<sup>59</sup> F. Sandrelli,<sup>59</sup> J. Walsh,<sup>59</sup> M. Haire,<sup>60</sup> D. Judd,<sup>60</sup>  
 K. Paick,<sup>60</sup> D. E. Wagoner,<sup>60</sup> N. Danielson,<sup>61</sup> P. Elmer,<sup>61</sup> Y. P. Lau,<sup>61</sup> C. Lu,<sup>61</sup> V. Miftakov,<sup>61</sup> J. Olsen,<sup>61</sup>  
 A. J. S. Smith,<sup>61</sup> A. V. Telnov,<sup>61</sup> F. Bellini,<sup>62</sup> G. Cavoto,<sup>61,62</sup> R. Faccini,<sup>62</sup> F. Ferrarotto,<sup>62</sup> F. Ferroni,<sup>62</sup>  
 M. Gaspero,<sup>62</sup> L. Li Gioi,<sup>62</sup> M. A. Mazzoni,<sup>62</sup> S. Morganti,<sup>62</sup> M. Pierini,<sup>62</sup> G. Piredda,<sup>62</sup> F. Safai Tehrani,<sup>62</sup>  
 C. Voena,<sup>62</sup> S. Christ,<sup>63</sup> G. Wagner,<sup>63</sup> R. Walldi,<sup>63</sup> T. Adye,<sup>64</sup> N. De Groot,<sup>64</sup> B. Franek,<sup>64</sup> N. I. Geddes,<sup>64</sup>  
 G. P. Gopal,<sup>64</sup> E. O. Olaiya,<sup>64</sup> R. Aleksan,<sup>65</sup> S. Emery,<sup>65</sup> A. Gaidot,<sup>65</sup> S. F. Ganzhur,<sup>65</sup> P.-F. Giraud,<sup>65</sup>  
 G. Hamel de Monchenault,<sup>65</sup> W. Kozanecki,<sup>65</sup> M. Legendre,<sup>65</sup> G. W. London,<sup>65</sup> B. Mayer,<sup>65</sup> G. Schott,<sup>65</sup>  
 G. Vasseur,<sup>65</sup> Ch. Yèche,<sup>65</sup> M. Zito,<sup>65</sup> M. V. Purohit,<sup>66</sup> A. W. Weidemann,<sup>66</sup> J. R. Wilson,<sup>66</sup> F. X. Yumiceva,<sup>66</sup>  
 D. Aston,<sup>67</sup> R. Bartoldus,<sup>67</sup> N. Berger,<sup>67</sup> A. M. Boyarski,<sup>67</sup> O. L. Buchmueller,<sup>67</sup> R. Claus,<sup>67</sup> M. R. Convery,<sup>67</sup>  
 M. Cristinziani,<sup>67</sup> G. De Nardo,<sup>67</sup> D. Dong,<sup>67</sup> J. Dorfan,<sup>67</sup> D. Dujmic,<sup>67</sup> W. Dunwoodie,<sup>67</sup> E. E. Elsen,<sup>67</sup> S. Fan,<sup>67</sup>  
 R. C. Field,<sup>67</sup> T. Glanzman,<sup>67</sup> S. J. Gowdy,<sup>67</sup> T. Hadig,<sup>67</sup> V. Halyo,<sup>67</sup> C. Hast,<sup>67</sup> T. Hryn'ova,<sup>67</sup> W. R. Innes,<sup>67</sup>  
 M. H. Kelsey,<sup>67</sup> P. Kim,<sup>67</sup> M. L. Kocian,<sup>67</sup> D. W. G. S. Leith,<sup>67</sup> J. Libby,<sup>67</sup> S. Luitz,<sup>67</sup> V. Luth,<sup>67</sup> H. L. Lynch,<sup>67</sup>  
 H. Marsiske,<sup>67</sup> R. Messner,<sup>67</sup> D. R. Muller,<sup>67</sup> C. P. O'Grady,<sup>67</sup> V. E. Ozcan,<sup>67</sup> A. Perazzo,<sup>67</sup> M. Perl,<sup>67</sup>  
 S. Petrak,<sup>67</sup> B. N. Ratcliff,<sup>67</sup> A. Roodman,<sup>67</sup> A. A. Salnikov,<sup>67</sup> R. H. Schindler,<sup>67</sup> J. Schwiening,<sup>67</sup> G. Simi,<sup>67</sup>  
 A. Snyder,<sup>67</sup> A. Soha,<sup>67</sup> J. Stelzer,<sup>67</sup> D. Su,<sup>67</sup> M. K. Sullivan,<sup>67</sup> J. Va'vra,<sup>67</sup> S. R. Wagner,<sup>67</sup> M. Weaver,<sup>67</sup>  
 A. J. R. Weinstein,<sup>67</sup> W. J. Wisniewski,<sup>67</sup> M. Wittgen,<sup>67</sup> D. H. Wright,<sup>67</sup> A. K. Yarritu,<sup>67</sup> C. C. Young,<sup>67</sup>  
 P. R. Burchat,<sup>68</sup> A. J. Edwards,<sup>68</sup> T. I. Meyer,<sup>68</sup> B. A. Petersen,<sup>68</sup> C. Roat,<sup>68</sup> S. Ahmed,<sup>69</sup> M. S. Alam,<sup>69</sup>  
 J. A. Ernst,<sup>69</sup> M. A. Saeed,<sup>69</sup> M. Saleem,<sup>69</sup> F. R. Wappler,<sup>69</sup> W. Bugg,<sup>70</sup> M. Krishnamurthy,<sup>70</sup> S. M. Spanier,<sup>70</sup>  
 R. Eckmann,<sup>71</sup> H. Kim,<sup>71</sup> J. L. Ritchie,<sup>71</sup> A. Satpathy,<sup>71</sup> R. F. Schwitters,<sup>71</sup> J. M. Izen,<sup>72</sup> I. Kitayama,<sup>72</sup>  
 X. C. Lou,<sup>72</sup> S. Ye,<sup>72</sup> F. Bianchi,<sup>73</sup> M. Bona,<sup>73</sup> F. Gallo,<sup>73</sup> D. Gamba,<sup>73</sup> L. Bosisio,<sup>74</sup> C. Cartaro,<sup>74</sup> F. Cossutti,<sup>74</sup>  
 G. Della Ricca,<sup>74</sup> S. Dittongo,<sup>74</sup> S. Grancagnolo,<sup>74</sup> L. Lanceri,<sup>74</sup> P. Poropat,<sup>74,§</sup> L. Vitale,<sup>74</sup> G. Vuagnin,<sup>74</sup>  
 R. S. Panvini,<sup>75</sup> Sw. Banerjee,<sup>76</sup> C. M. Brown,<sup>76</sup> D. Fortin,<sup>76</sup> P. D. Jackson,<sup>76</sup> R. Kowalewski,<sup>76</sup> J. M. Roney,<sup>76</sup>  
 R. J. Sobie,<sup>76</sup> H. R. Band,<sup>77</sup> B. Cheng,<sup>77</sup> S. Dasu,<sup>77</sup> M. Datta,<sup>77</sup> A. M. Eichenbaum,<sup>77</sup> M. Graham,<sup>77</sup> J. J. Hollar,<sup>77</sup>  
 J. R. Johnson,<sup>77</sup> P. E. Kutter,<sup>77</sup> H. Li,<sup>77</sup> R. Liu,<sup>77</sup> A. Mihalyi,<sup>77</sup> A. K. Mohapatra,<sup>77</sup> Y. Pan,<sup>77</sup> R. Prepost,<sup>77</sup>  
 P. Tan,<sup>77</sup> J. H. von Wimmersperg-Toeller,<sup>77</sup> J. Wu,<sup>77</sup> S. L. Wu,<sup>77</sup> Z. Yu,<sup>77</sup> M. G. Greene,<sup>78</sup> and H. Neal<sup>78</sup>

(The BABAR Collaboration)

<sup>1</sup>Laboratoire de Physique des Particules, F-74941 Annecy-le-Vieux, France

<sup>2</sup>Università di Bari, Dipartimento di Fisica and INFN, I-70126 Bari, Italy

<sup>3</sup>Institute of High Energy Physics, Beijing 100039, China

<sup>4</sup>University of Bergen, Inst. of Physics, N-5007 Bergen, Norway

<sup>5</sup>Lawrence Berkeley National Laboratory and University of California, Berkeley, CA 94720, USA

<sup>6</sup>University of Birmingham, Birmingham, B15 2TT, United Kingdom

<sup>7</sup>Ruhr Universität Bochum, Institut für Experimentalphysik 1, D-44780 Bochum, Germany

<sup>8</sup>University of Bristol, Bristol BS8 1TL, United Kingdom

<sup>9</sup>University of British Columbia, Vancouver, BC, Canada V6T 1Z1

<sup>10</sup>Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom

<sup>11</sup>Budker Institute of Nuclear Physics, Novosibirsk 630090, Russia

<sup>12</sup>University of California at Irvine, Irvine, CA 92697, USA

<sup>13</sup>University of California at Los Angeles, Los Angeles, CA 90024, USA

<sup>14</sup>University of California at Riverside, Riverside, CA 92521, USA

<sup>15</sup>University of California at San Diego, La Jolla, CA 92093, USA

- <sup>16</sup> University of California at Santa Barbara, Santa Barbara, CA 93106, USA
- <sup>17</sup> University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, CA 95064, USA
- <sup>18</sup> California Institute of Technology, Pasadena, CA 91125, USA
- <sup>19</sup> University of Cincinnati, Cincinnati, OH 45221, USA
- <sup>20</sup> University of Colorado, Boulder, CO 80309, USA
- <sup>21</sup> Colorado State University, Fort Collins, CO 80523, USA
- <sup>22</sup> Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany
- <sup>23</sup> Ecole Polytechnique, LLR, F-91128 Palaiseau, France
- <sup>24</sup> University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom
- <sup>25</sup> Università di Ferrara, Dipartimento di Fisica and INFN, I-44100 Ferrara, Italy
- <sup>26</sup> Florida A&M University, Tallahassee, FL 32307, USA
- <sup>27</sup> Laboratori Nazionali di Frascati dell'INFN, I-00044 Frascati, Italy
- <sup>28</sup> Università di Genova, Dipartimento di Fisica and INFN, I-16146 Genova, Italy
- <sup>29</sup> Harvard University, Cambridge, MA 02138, USA
- <sup>30</sup> Universität Heidelberg, Physikalisches Institut, Philosophenweg 12, D-69120 Heidelberg, Germany
- <sup>31</sup> Imperial College London, London, SW7 2AZ, United Kingdom
- <sup>32</sup> University of Iowa, Iowa City, IA 52242, USA
- <sup>33</sup> Iowa State University, Ames, IA 50011-3160, USA
- <sup>34</sup> Università di Perugia, Dipartimento di Fisica and INFN, I-06100 Perugia, Italy
- <sup>35</sup> Laboratoire de l'Accélérateur Linéaire, F-91898 Orsay, France
- <sup>36</sup> Lawrence Livermore National Laboratory, Livermore, CA 94550, USA
- <sup>37</sup> University of Liverpool, Liverpool L69 7ZE, United Kingdom
- <sup>38</sup> Queen Mary, University of London, E1 4NS, United Kingdom
- <sup>39</sup> University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom
- <sup>40</sup> University of Louisville, Louisville, KY 40292, USA
- <sup>41</sup> University of Manchester, Manchester M13 9PL, United Kingdom
- <sup>42</sup> University of Maryland, College Park, MD 20742, USA
- <sup>43</sup> University of Massachusetts, Amherst, MA 01003, USA
- <sup>44</sup> Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, MA 02139, USA
- <sup>45</sup> McGill University, Montréal, QC, Canada H3A 2T8
- <sup>46</sup> Università di Milano, Dipartimento di Fisica and INFN, I-20133 Milano, Italy
- <sup>47</sup> University of Mississippi, University, MS 38677, USA
- <sup>48</sup> Université de Montréal, Laboratoire René J. A. Lévesque, Montréal, QC, Canada H3C 3J7
- <sup>49</sup> Mount Holyoke College, South Hadley, MA 01075, USA
- <sup>50</sup> Università di Napoli Federico II, Dipartimento di Scienze Fisiche and INFN, I-80126, Napoli, Italy
- <sup>51</sup> NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands
- <sup>52</sup> University of Notre Dame, Notre Dame, IN 46556, USA
- <sup>53</sup> Ohio State University, Columbus, OH 43210, USA
- <sup>54</sup> University of Oregon, Eugene, OR 97403, USA
- <sup>55</sup> Università di Padova, Dipartimento di Fisica and INFN, I-35131 Padova, Italy
- <sup>56</sup> Universités Paris VI et VII, Laboratoire de Physique Nucléaire et de Hautes Energies, F-75252 Paris, France
- <sup>57</sup> Università di Pavia, Dipartimento di Elettronica and INFN, I-27100 Pavia, Italy
- <sup>58</sup> University of Pennsylvania, Philadelphia, PA 19104, USA
- <sup>59</sup> Università di Pisa, Dipartimento di Fisica, Scuola Normale Superiore and INFN, I-56127 Pisa, Italy
- <sup>60</sup> Prairie View A&M University, Prairie View, TX 77446, USA
- <sup>61</sup> Princeton University, Princeton, NJ 08544, USA
- <sup>62</sup> Università di Roma La Sapienza, Dipartimento di Fisica and INFN, I-00185 Roma, Italy
- <sup>63</sup> Universität Rostock, D-18051 Rostock, Germany
- <sup>64</sup> Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom
- <sup>65</sup> DSM/Dapnia, CEA/Saclay, F-91191 Gif-sur-Yvette, France
- <sup>66</sup> University of South Carolina, Columbia, SC 29208, USA
- <sup>67</sup> Stanford Linear Accelerator Center, Stanford, CA 94309, USA
- <sup>68</sup> Stanford University, Stanford, CA 94305-4060, USA
- <sup>69</sup> State University of New York, Albany, NY 12222, USA
- <sup>70</sup> University of Tennessee, Knoxville, TN 37996, USA
- <sup>71</sup> University of Texas at Austin, Austin, TX 78712, USA
- <sup>72</sup> University of Texas at Dallas, Richardson, TX 75083, USA
- <sup>73</sup> Università di Torino, Dipartimento di Fisica Sperimentale and INFN, I-10125 Torino, Italy
- <sup>74</sup> Università di Trieste, Dipartimento di Fisica and INFN, I-34127 Trieste, Italy
- <sup>75</sup> Vanderbilt University, Nashville, TN 37235, USA
- <sup>76</sup> University of Victoria, Victoria, BC, Canada V8W 3P6
- <sup>77</sup> University of Wisconsin, Madison, WI 53706, USA
- <sup>78</sup> Yale University, New Haven, CT 06511, USA

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Branching fraction measurements using  $B$ -meson decays to  $K_s^0\pi^+\pi^-$  are presented. These measurements were obtained by analyzing a data sample of 88.9 million  $\Upsilon(4S) \rightarrow B\bar{B}$  decays collected with the *BABAR* detector at the SLAC PEP-II asymmetric-energy  $B$  factory. Using a maximum likelihood fit, the following branching fraction results were obtained:  $\mathcal{B}(B^0 \rightarrow K^0\pi^+\pi^-) = (43.7 \pm 3.8 \pm 3.4) \times 10^{-6}$ ,  $\mathcal{B}(B^0 \rightarrow K^{*+}\pi^-) = (12.9 \pm 2.4 \pm 1.4) \times 10^{-6}$  and  $\mathcal{B}(B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+) = (42.7 \pm 2.1 \pm 2.2) \times 10^{-6}$ . The  $CP$  violating charge asymmetry  $\mathcal{A}_{K^*\pi}$  for the decay  $B^0 \rightarrow K^{*+}\pi^-$  was measured to be  $\mathcal{A}_{K^*\pi} = 0.23 \pm 0.18^{+0.09}_{-0.06}$ . For all these measurements the first error is statistical and the second is systematic.

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Three-body decays of the  $B$  meson tend to be dominated by intermediate quasi two-body charmed particles with the charmless resonant and non-resonant contribution being small. Nevertheless, these charmless decays prove to be important in furthering our understanding of the weak interaction and complex quark couplings described by the Cabibbo-Kobayashi-Maskawa matrix elements [1].

The  $B$ -meson decay to  $K_s^0\pi^+\pi^-$  can proceed via many interesting charmless resonances which we can probe for  $CP$  violation, such as  $f_0K_s^0$  [2],  $\rho^0K_s^0$  and  $K^{*+}\pi^-$ . A limit on the sum of their branching fractions can be obtained by measuring the inclusive charmless branching fraction of  $B^0 \rightarrow K_s^0\pi^+\pi^-$ . This measurement has been performed previously by the CLEO [3] and Belle [4] experiments. For the mode  $B^0 \rightarrow K^{*+}\pi^-$  the branching fraction can be measured directly with the available *BABAR* data sample.

Branching fraction and asymmetry measurements of charmless  $B$  decays can also be used to test the accuracy of QCD factorization models [5]. In particular there are factorization models that predict  $CP$  asymmetries in the decay  $B^0 \rightarrow K^{*+}\pi^-$  [6]. The decay  $B^0 \rightarrow K^{*+}\pi^-$  is self tagged (the charge of the kaon reflects the flavor of the  $B$ -meson), so the  $CP$  asymmetry can be defined as:

$$\mathcal{A}_{K^*\pi} = \frac{\Gamma_{K^{*-}\pi^+} - \Gamma_{K^{*+}\pi^-}}{\Gamma_{K^{*-}\pi^+} + \Gamma_{K^{*+}\pi^-}}. \quad (1)$$

In this paper the branching fractions of  $B^0 \rightarrow K^0\pi^+\pi^-$ ,  $B^0 \rightarrow K^{*+}\pi^-$  and  $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$  are presented, where charge conjugate decays are also implied. The procedure used selection criteria requiring events with a reconstructed  $K_s^0\pi^+\pi^-$  final state. In the case of  $\mathcal{B}(B^0 \rightarrow K^0\pi^+\pi^-)$ , the total charmless contribution to the Dalitz plot was measured (with charmed and charmonium resonances removed), including contributions from resonant charmless sub-structure. For the decays  $B^0 \rightarrow K^{*+}\pi^-$  and  $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$ , the analysis was restricted to the region of the  $K_s^0\pi^+\pi^-$  Dalitz plot consistent with  $K^{*+}(\rightarrow K_s^0\pi^+)$  and  $D^-(\rightarrow K_s^0\pi^-)$  decays respectively. Finally, the  $\mathcal{A}_{K^*\pi}$  value for the decay  $B^0 \rightarrow K^{*+}\pi^-$ , which was first measured by CLEO [7] was extracted.

The data used in this analysis were collected at the PEP-II asymmetric-energy  $e^+e^-$  storage ring with

the *BABAR* detector [8]. The *BABAR* detector consists of a double-sided five-layer silicon tracker, a 40-layer drift chamber, a Cherenkov detector, an electromagnetic calorimeter and a magnet with instrumented flux return. The data sample has an integrated luminosity of  $81.9 \text{ fb}^{-1}$  collected at the  $\Upsilon(4S)$  resonance, which corresponds to  $(88.9 \pm 1.0) \times 10^6 B\bar{B}$  pairs. It was assumed that the  $\Upsilon(4S)$  decays equally to neutral and charged  $B$ -meson pairs. In addition,  $9.6 \text{ fb}^{-1}$  of data collected at 40 MeV below the  $\Upsilon(4S)$  resonance were used for background studies.

Candidate  $B$ -mesons were reconstructed from two tracks and a  $K_s^0$ , where the  $K_s^0$  was reconstructed from  $\pi^+\pi^-$  candidates. Each of the two tracks that were not generated by the  $K_s^0$  were required to have at least 12 hits in the drift chamber, a transverse momentum greater than 100 MeV/ $c$  and to be consistent with originating from the beam-spot. These tracks were selected as pions using energy loss ( $dE/dx$ ) measured in the tracking system, the number of photons measured by the Cherenkov detector and their corresponding Cherenkov angle. Furthermore, the tracks were also required to fail the electron selection based on  $dE/dx$  information, the ratio of energy in the calorimeter to momentum in the drift chamber and the shape of the signal in the calorimeter. The prerequisites imposed on  $K_s^0$  candidates were for the reconstructed mass to be within 15 MeV/ $c^2$  of the nominal  $K^0$  mass [9], a decay vertex separated from the  $B^0$  decay vertex by at least five standard deviations and a cosine of the angle between the line joining the  $B$  and  $K_s^0$  decay vertices and the  $K_s^0$  momentum to be greater than 0.999.

To characterize signal events, two kinematic and one event shape variable were used. The first kinematic variable  $\Delta E$ , is the difference between the center-of-mass (CM) energy of the  $B$ -candidate and  $\sqrt{s}/2$ , where  $\sqrt{s}$  is the total CM energy. The second is the beam-energy-substituted mass  $m_{\text{ES}} = \sqrt{(s/2 + \mathbf{p}_i \cdot \mathbf{p}_B)^2/E_i^2 - \mathbf{p}_B^2}$ , where  $\mathbf{p}_B$  is the  $B$  momentum and  $(E_i, \mathbf{p}_i)$  is the four-momentum of the  $\Upsilon(4S)$  in the laboratory frame. Using these two kinematic variables, candidates had to be in the range  $|\Delta E| < 0.1 \text{ GeV}$  and  $5.22 < m_{\text{ES}} < 5.29 \text{ GeV}/c^2$ . The event shape variable is a Fisher discriminant ( $\mathcal{F}$ ) [10]. The  $\mathcal{F}$  variable was constructed from a linear combination of the cosine of the angle between the  $B$ -candidate momentum and the beam axis, the co-

sine of the angle between the  $B$ -candidate thrust axis and the beam axis, and the energy flow of the rest of the event into each of nine contiguous, concentric,  $10^\circ$  cones around the thrust axis of the reconstructed  $B$  [11].

Continuum quark production ( $e^+e^- \rightarrow q\bar{q}$  where  $q = u, d, s, c$ ) was by far the dominant source of background. This was suppressed using another event-shape variable which was the cosine of the angle  $\theta_T$  between the thrust axis of the selected  $B$ -candidate and the thrust axis of the rest of the event. For continuum background, the distribution of  $|\cos\theta_T|$  is strongly peaked towards unity whereas the distribution is flat for signal events. Therefore, the relative amount of continuum background was reduced by requiring that all candidates fulfill the criterion  $|\cos\theta_T| < 0.9$ .

Simulated Monte Carlo (MC) events were used to study background from other  $B$ -meson decays. The largest potential  $B$ -background was seen to come from quasi two-body decays including charmonium mesons such as  $J/\psi K_s^0$ ,  $\chi_{c0} K_s^0$  and  $\psi(2S) K_s^0$  where the charmonium meson decays to  $\mu^+\mu^-$  which are misidentified as pions or where they decay directly to  $\pi^+\pi^-$ . These background events were removed by vetoing reconstructed  $\pi^+\pi^-$  masses consistent with  $3.04 < m_{\pi^+\pi^-} < 3.17$  GeV/ $c^2$ ,  $3.32 < m_{\pi^+\pi^-} < 3.53$  GeV/ $c^2$  and  $3.60 < m_{\pi^+\pi^-} < 3.78$  GeV/ $c^2$ , identifying the  $J/\psi$ ,  $\chi_{c0}$  and  $\psi(2S)$  mesons respectively. Additionally, in order to measure the charmless branching fraction of the decay  $B^0 \rightarrow K^0\pi^+\pi^-$ ,  $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$  events were removed by vetoing events with a reconstructed  $K_s^0\pi$  invariant mass consistent with  $1.83 < m_{K_s^0\pi} < 1.90$  GeV/ $c^2$ . Monte Carlo simulation showed that  $21 \pm 3$   $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$  background events still remained. These events had a reconstructed  $D^-$  mass outside the veto as a result of using the wrong  $K_s^0$  or  $\pi^+$  which was incorrectly selected from the other  $B$  decay in the event. When selecting  $B^0 \rightarrow K^{*+}\pi^-$  or  $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$  candidates, the additional cuts  $0.79 < m_{K_s^0\pi} < 0.99$  GeV/ $c^2$  and  $1.85 < m_{K_s^0\pi} < 1.89$  GeV/ $c^2$  were applied respectively to the reconstructed  $m_{K_s^0\pi}$  invariant mass. After the above selection criteria were applied, a small proportion of events for all decays under study had more than one candidate which satisfied the selection criteria. For these events, one candidate alone was selected by choosing the candidate whose  $\cos\theta_T$  value was closest to 0. In a signal MC study, this selects the true signal candidate more than 75% of the time.

After all cuts, the largest remaining  $B$ -background to  $B^0 \rightarrow K^0\pi^+\pi^-$  was the 4-body decay  $B^0 \rightarrow \eta' K_s^0$  with  $\eta' \rightarrow \rho^0(770)\gamma$  and  $\rho^0 \rightarrow \pi^+\pi^-$  which contributes  $22 \pm 6$  events. For the  $B^0 \rightarrow K^{*+}\pi^-$  and  $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$  channels, the background contribution was small and came from modes that can interfere by decaying to a  $K_s^0\pi^+\pi^-$  final state such as  $f_0 K_s^0$  and  $\rho^0 K_s^0$ . In addition the  $K^{*+}\pi^-$  and  $D^+\pi^-$  modes are backgrounds to each other. Furthermore, there was the

non-resonant  $K_s^0\pi^+\pi^-$  background contribution to the resonant signal. Along with selection efficiencies obtained from MC, using available information on exclusive measurements [12] or by fitting to regions in the Dalitz plot, upper limits or branching fractions for these modes were obtained to estimate their background contributions.

In order to extract the signal event yield for the channel under study, an unbinned extended maximum likelihood fit was used. The likelihood function for  $N$  candidates is:

$$\mathcal{L} = \exp\left(-\sum_{i=1}^M n_i\right) \prod_{j=1}^N \left(\sum_{l=1}^M n_l P_l(\vec{\alpha}, \vec{x}_j)\right), \quad (2)$$

where  $i, j$  and  $l$  are integers,  $M$  is the number of hypotheses (signal, continuum background and  $B$ -background),  $P_l(\vec{\alpha}, \vec{x}_j)$  is a probability density function (PDF) with the parameters  $\vec{\alpha}$  depending on three variables ( $\vec{x}$ )  $m_{ES}$ ,  $\Delta E$ , and  $\mathcal{F}$ , and  $n_l$  is the number of events for each hypothesis determined by maximizing the likelihood function. The PDF is a product  $P_l(\vec{\alpha}, \vec{x}_j) = P_l(\alpha_{m_{ES}}, m_{ES}) \cdot P_l(\alpha_{\Delta E}, \Delta E) \cdot P_l(\alpha_{\mathcal{F}}, \mathcal{F})$ . Correlations between these variables were small for signal and continuum background hypotheses. However for  $B$ -background, correlations were observed between  $m_{ES}$  and  $\Delta E$ , which were taken into account by forming a 2-dimensional PDF for these variables. The parameters of the signal and  $B$ -background PDFs were determined from MC. The continuum background parameters were allowed to vary in the fit, to help reduce systematic effects from this dominant event type. Upper sideband data defined to be in the region  $0.1 < \Delta E < 0.3$  GeV and  $5.22 < m_{ES} < 5.29$  GeV/ $c^2$  was used to model the continuum background PDFs. For the  $m_{ES}$  PDFs a Gaussian distribution was used for signal and a threshold function [13] was used for continuum. For the  $\Delta E$  PDFs a sum of two Gaussian distributions with the same means was used for the signal and a first order polynomial was used for the continuum background. Finally, for the  $\mathcal{F}$  PDFs, a sum of two Gaussian distributions with distinct means and widths was used for signal and an asymmetric Gaussian which has different widths above and below the modal value was used for continuum background. In the case of  $B$ -background parameterizations, signal-like or continuum-like PDFs were used depending on the characteristics of the background. With more than 400 signal events and typically a one-to-one signal to background ratio in the total number of  $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$  candidates, it was possible also to vary the signal PDF parameters in the fit for this mode. This enabled uncertainties and corrections due to MC, to be calculated and applied to the  $B^0 \rightarrow K^0\pi^+\pi^-$  and  $B^0 \rightarrow K^{*+}\pi^-$  analyses. Figure 1 shows the fitted projections of the maximum likelihood fit to  $B^0 \rightarrow D^-(\rightarrow K_s^0\pi^-)\pi^+$  candidates in  $m_{ES}$ ,  $\Delta E$  and  $\mathcal{F}$  containing  $472 \pm 24$  signal and  $455 \pm 23$  background candidates.

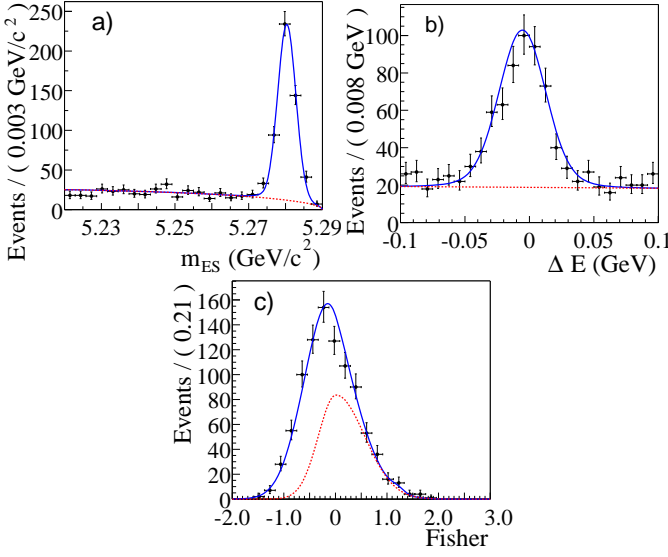


FIG. 1: Maximum likelihood fit projections of  $m_{ES}$  (a),  $\Delta E$  (b) and  $\mathcal{F}$  (c) to the full set of  $B^0 \rightarrow D^- (\rightarrow K_S^0 \pi^-) \pi^+$  candidates. The dashed line is the fitted background PDF while the solid continuous line is the sum of the signal and background PDFs. The solid dots are data used in the fit.

To extract the branching fractions for the decay modes  $B^0 \rightarrow K^{*+} \pi^-$  and  $B^0 \rightarrow D^- (\rightarrow K_S^0 \pi^-) \pi^+$  the following equation was used:

$$\mathcal{B} = \frac{n_{sig}}{N_{BB} \times \epsilon}, \quad (3)$$

where  $n_{sig}$  is the number of signal events fitted,  $\epsilon$  is the signal efficiency obtained from MC and  $N_{BB}$  is the total number of  $B\bar{B}$  events. For the charmless inclusive  $B^0 \rightarrow K^0 \pi^+ \pi^-$  branching fraction, the efficiency varies over the Dalitz plane and the distribution of events across it is *a priori* unknown, consequently the total efficiency is unknown. Therefore, to calculate the branching fraction, a weight was assigned to each event such that, for the  $j$ th event  $\mathcal{W}_j = \sum_i V_{sig,i} P_i(\vec{\alpha}, \vec{x}_j) / \sum_k n_k P_k(\vec{\alpha}, \vec{x}_j)$  where  $V_{sig,i}$  is the signal row of the covariance matrix obtained from the fit [14]. This procedure is effectively a background subtraction where these weights have the property  $\sum_j \mathcal{W}_j = n_{sig}$ . The branching fraction is then calculated as  $\mathcal{B} = \sum_j \mathcal{W}_j / (\epsilon_j \times N_{BB})$  where  $\epsilon_j$  is the efficiency which varies across the Dalitz plot and is simulated in small bins using high statistics MC.

Figure 2 shows the fitted projections for both  $B^0 \rightarrow K^0 \pi^+ \pi^-$  and  $B^0 \rightarrow K^{*+} \pi^-$  candidates, whilst the fitted signal yield and measured branching fraction are shown in Table I for all the modes under study. The average efficiency for  $B^0 \rightarrow K^0 \pi^+ \pi^-$  signal events was approximately 8%. Figure 3 shows the signal mass projections of  $m_{K_S^0 \pi}$  using  $B^0 \rightarrow K^0 \pi^+ \pi^-$  candidates. The  $m_{K_S^0 \pi}$  distribution clearly shows a peak at 0.9 GeV/c<sup>2</sup> which corresponds to the  $K^{*+}(892)$  and there is a broad struc-

ture above 1 GeV/c<sup>2</sup> which is the region where higher kaon resonances can occur.

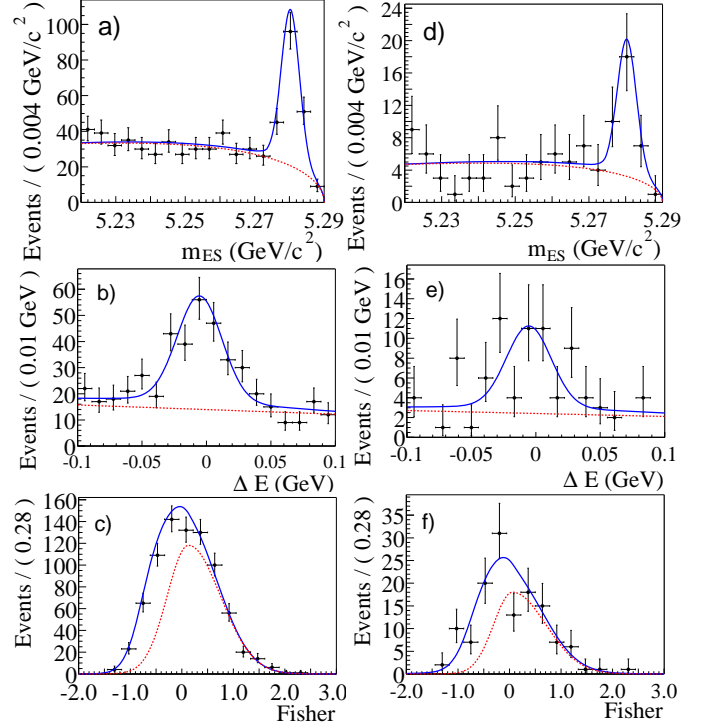


FIG. 2: Maximum likelihood fit projections of  $m_{ES}$ ,  $\Delta E$  and  $\mathcal{F}$  for signal enhanced samples of charmless  $B^0 \rightarrow K^0 \pi^+ \pi^-$  and  $B^0 \rightarrow K^{*+} \pi^-$  candidates. The dashed line is the fitted background PDF while the solid continuous line is the sum of the signal and background PDFs. The solid dots are data. The left column (plots a-c) has the  $B^0 \rightarrow K^0 \pi^+ \pi^-$  projections and the right column (plots d-f) has the  $B^0 \rightarrow K^{*+} \pi^-$  projections, the top, middle and bottom rows being the  $m_{ES}$ ,  $\Delta E$  and  $\mathcal{F}$  distributions respectively.

TABLE I: Signal yields and branching fractions for  $B^0 \rightarrow K^0 \pi^+ \pi^-$ ,  $B^0 \rightarrow K^{*+} \pi^-$  and  $B^0 \rightarrow D^- (\rightarrow K_S^0 \pi^-) \pi^+$  where the first error is statistical and in the case of the branching fraction measurements the second error is systematic. The efficiency of selecting  $B^0 \rightarrow K^{*+} \pi^-$  and  $B^0 \rightarrow D^- (\rightarrow K_S^0 \pi^-) \pi^+$  events was found to be 5.1% and 12.4% respectively. The  $B^0 \rightarrow K^{*+} \pi^-$  branching fraction takes into account that  $\mathcal{B}(K^{*+} \rightarrow K^0 \pi^+) = 2/3$ , assuming isospin symmetry.

Mode	Signal Events Yield	Branching Fraction ( $\times 10^{-6}$ )
$B^0 \rightarrow K^0 \pi^+ \pi^-$	$310 \pm 27$	$43.7 \pm 3.8 \pm 3.4$
$B^0 \rightarrow K^{*+} \pi^-$	$59 \pm 11$	$12.9 \pm 2.4 \pm 1.4$
$B^0 \rightarrow D^- (\rightarrow K_S^0 \pi^-) \pi^+$	$472 \pm 24$	$42.7 \pm 2.1 \pm 2.2$

Contributions to the branching fraction systematic error are shown in Table II. Errors due to pion tracking, particle identification and  $K_S^0$  reconstruction efficiency

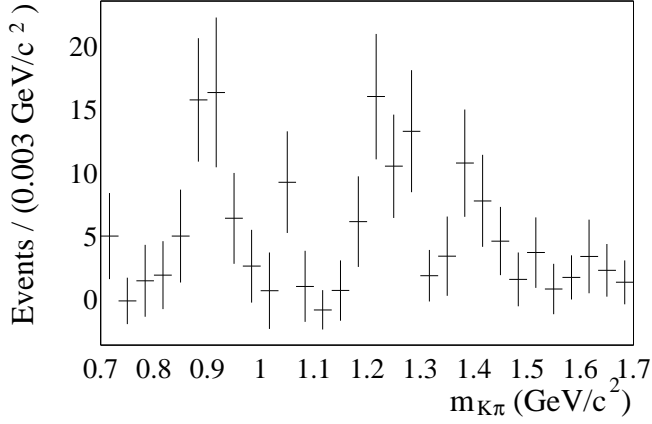


FIG. 3: The  $m_{K\pi}$  distribution of  $B^0 \rightarrow K^0 \pi^+ \pi^-$  candidates, weighted by  $\mathcal{W}$  such that background events are subtracted. The one-dimensional distribution is obtained by considering events on a Dalitz plane with axes  $m_{K_S^0 \pi^+}^2$  and  $m_{K_S^0 \pi^-}^2$ . The two axes are merged into one ( $m_{K\pi}^2$ ) by folding the Dalitz plane along the line corresponding to  $m_{K_S^0 \pi^+}^2 = m_{K_S^0 \pi^-}^2$  in order to obtain the above  $m_{K\pi}$  mass distribution.

were assigned by comparing control channels in MC and data. To calculate errors due to the fit procedure, a large number of MC samples containing the amounts of signal, continuum and  $B$ -background events measured or fixed in data were used. The differences between the generated and fitted values using these samples were used to ascertain the sizes of any biases. Small biases of the order of a few percent were observed that were a consequence of small correlations between fit variables and were therefore assigned as systematic errors. The uncertainty of the  $B$ -background contribution to the fit was estimated by varying the measured branching fractions within their errors. Each background was varied individually and the effect on the fitted signal yield was added as a contribution to the uncertainty. For  $B^0 \rightarrow K^{*+} \pi^-$  there was also the  $B$ -background contributions from higher kaon resonances which was obtained from fits to data and added as a systematic. The uncertainty due to simulated PDFs was obtained from the channel  $B^0 \rightarrow D^-(\rightarrow K_S^0 \pi^-) \pi^+$  and by varying the PDFs according to the precision of the parameters obtained from MC. In order to take correlations between parameters into account, the full correlation matrix was used when varying parameters. All PDF parameters that were originally fixed in the fit were then varied in turn and each difference from the nominal fit was combined and taken as a systematic contribution. The error in the efficiency was due to limited MC statistics, where over a million MC events were generated for the decay  $B^0 \rightarrow K^0 \pi^+ \pi^-$  and over one hundred and fifty thousand MC events were generated for the decays  $B^0 \rightarrow K^{*+} \pi^-$  and  $B^0 \rightarrow D^-(\rightarrow K_S^0 \pi^-) \pi^+$ . The same uncertainty due to the error in the number of  $B\bar{B}$  events was added to all channels.

TABLE II: Summary of systematic uncertainty contributions to the branching fraction measurements  $B^0 \rightarrow K^0 \pi^+ \pi^-$ ,  $B^0 \rightarrow K^{*+} \pi^-$  and  $B^0 \rightarrow D^-(\rightarrow K_S^0 \pi^-) \pi^+$ . The errors are shown as a percentage of the measured branching fraction.

Error source	$B^0 \rightarrow K^0 \pi^+ \pi^-$ error(%)	$B^0 \rightarrow K^{*+} \pi^-$ error(%)	$B^0 \rightarrow D^-(\rightarrow K_S^0 \pi^-) \pi^+$ error (%)
Tracking	1.7	1.7	1.7
Particle ID	1.9	1.2	3.0
$K_S^0$ Efficiency	4.2	3.5	3.0
Fit Bias	4.1	3.3	1.8
$B$ -background	3.6	9.0	0.3
PDF params.	1.5	0.5	0.4
Efficiency	1.7	0.6	0.6
No. of $B\bar{B}$	1.1	1.1	1.1
Total	7.8	10.5	5.1

Interference was also considered for the decay  $B^0 \rightarrow K^{*+} \pi^-$  where effects between the  $K^{*+}(892)$  and S wave final states (non-resonant and  $K_0^{*+}(1430)$ ) cancel and the  $K^{*+}(892)$  and D wave final states ( $K_2^{*+}(1430)$ ) cancel. This is not the case for P wave amplitudes such as  $K_1^{*+}(1410)$ , yet this effect was considered negligible due to the small branching fraction of  $K_1^{*+}(1410) \rightarrow K_S^0 \pi^+$  ( $6.6 \pm 1.3\%$  [9]).

The  $CP$  violating charge asymmetry for the decay  $B^0 \rightarrow K^{*+} \pi^-$  was measured to be  $\mathcal{A}_{K^* \pi} = 0.23 \pm 0.18^{+0.09}_{-0.06}$ , where the first error is statistical and the second errors are systematic. The background asymmetry  $\mathcal{A}_{K^* \pi}^{Bkg}$  was measured to be  $0.01 \pm 0.01$  and as a further study the asymmetry  $\mathcal{A}_{D\pi}$  for  $B^0 \rightarrow D^-(\rightarrow K_S^0 \pi^-) \pi^+$  was measured to be  $0.00 \pm 0.05$  and the background asymmetry  $\mathcal{A}_{D\pi}^{Bkg}$  was  $0.06 \pm 0.04$ , were the errors are statistical only.

The systematic error on  $\mathcal{A}_{K^* \pi}$  was calculated by considering contributions due to track finding, particle identification, fit biases and  $B$ -background asymmetry uncertainties. Biases due to track finding and particle identification were found to be negligible. The fit bias contribution to the systematic error was calculated using a large number of MC samples. The contribution from  $B$ -background was calculated by varying the number of expected events within errors and by assuming a conservative  $CP$  violating asymmetry of  $\pm 0.5$  as there are no available measurements for these decays. The resulting systematic uncertainty on the asymmetry was measured to be  $^{+0.09}_{-0.06}$ .

In summary, the branching fractions for  $B^0 \rightarrow K^0 \pi^+ \pi^-$ ,  $B^0 \rightarrow K^{*+} \pi^-$  and  $B^0 \rightarrow D^-(\rightarrow K_S^0 \pi^-) \pi^+$  decaying to a  $K_S^0 \pi^+ \pi^-$  state have been measured and agree with previous measurements [3, 4, 9]. The direct  $CP$  violating parameter  $\mathcal{A}_{K^* \pi}$  was measured for the decay  $B^0 \rightarrow K^{*+} \pi^-$  and is in agreement with the CLEO measurement [7], with no evidence of  $CP$  violation with the statistics used. Using larger datasets, one can extract amplitudes and relative phases of the resonant contribu-

tions to the Dalitz plot, with the possibility to observe new  $B$ -meson decays.

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\* Now at Department of Physics, University of Warwick, Coventry, United Kingdom

† Also with Università della Basilicata, Potenza, Italy

‡ Also with IFIC, Instituto de Física Corpuscular, CSIC-Universidad de Valencia, Valencia, Spain

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